

Language is a set of strings.

Language on Σ is a subset Σ^*
member 2^{Σ^*}

left-linear grammar

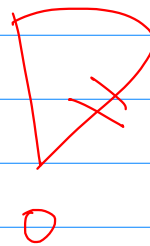
$A \rightarrow aB|c$

$A \rightarrow aB$

$A \rightarrow c$

A regular language is:

- DFA
- NFA
- left-linear grammar
- regular expression



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Context-free Language (CFL)

↳ Pushdown Automata (PDA)

↳ Context-free grammar (CFG)

Subset of 2^{Σ^*} = set of language
reg. expr $\subset 2^{\Sigma^*}$
reg. lang. $\in 2^{\Sigma^*}$



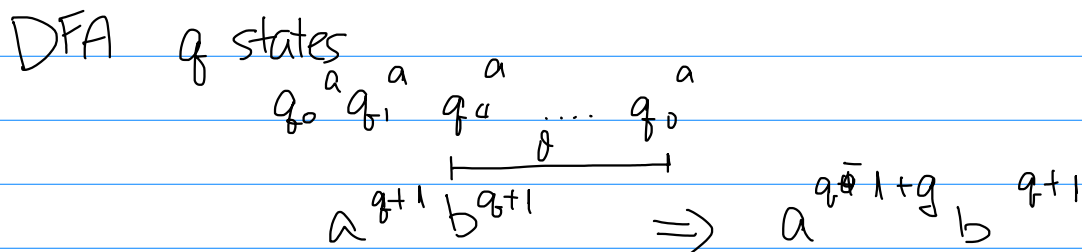
2

$$\text{Reg} = \{ a^k \mid k \geq 0 \}$$

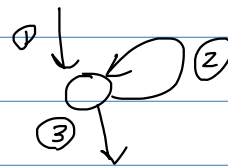
$$= \{ \varepsilon, a, aa, aaa, \dots \}$$

$$\text{Context-free} = \{ a^k b^k \mid k \geq 0 \}$$

$$= \{ \varepsilon, ab, aabb, aaabbb, \dots \}$$



Weird proof with Pigeon Hole Principle that shows contradiction



Context free grammar says : $\{ S \rightarrow \varepsilon \mid aSB \}$

0 recursively enumerable

1 Context-free language (context-sensitive)

Context-Free Grammar

$$G = (P, N, T, S)$$

grammar \nearrow P punctuation \nearrow N set of non-terminals \nearrow T set of terminals (bdd) \nearrow S start symbol \nwarrow $S \in N$

In a CFG production

$$A \rightarrow \alpha$$

$A \in N$ $\alpha \in (N \cup T \cup \{\epsilon\})^*$

$G =$

$$A \rightarrow B+B$$

$$A \rightarrow B$$

$$B \rightarrow C * C$$

$$B \rightarrow C$$

$$C \rightarrow d$$

$$C \rightarrow (A)$$

list of productions where left is the start symbol,

$N =$ set of capital letter = $\{A, B, C\}$

OR the LHS of the production

$T = \{+, *, (,)\}$

OR other stuff on RHS

Derivation using grammar G

start symbol

$$A \Rightarrow \bar{B} + B \Rightarrow \bar{C} + B \Rightarrow d + \bar{B} \Rightarrow d + C * \bar{C}$$

replaced with RHS of an A-production

choose one non-terminal and replace

$$\Rightarrow d + \bar{C} * d \Rightarrow d + d * d$$

no nonterminals
process ends !!

Right-most Derivation:

Any string that appears in a leftmost derivation is a left-sentential form \Rightarrow right most - right sentential

$$A \xRightarrow{*} d + (d * d) * d$$

↑
sentences only contain terminals

leftmost derivation

Top-down parsing is usually LL() parsing

read input from
left to right
(start) (end)

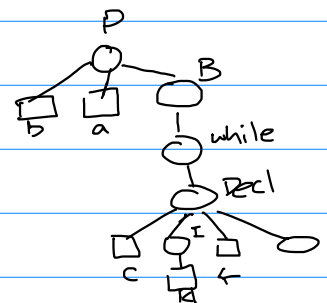
```
box main {  
  const x ← 2;  
  print x ;  
}
```

```
ParseProgram ()  
  expect ("box") ;  
  expect ("main") ;  
  parseBoxBody () ;
```

```
parseBoxBody ()  
  :
```

```
  while  
    parseStatement ()
```

```
parseStatement ()  
  parseDecl ()  
  parseDecl ()  
  expect ("const", "init")  
  parseIdentifier ()
```



Bottom-up Parsing is usually LR
 ↙ Rightmost derivation
 ↗ from left to right

Grammar

$$A \rightarrow A + A$$

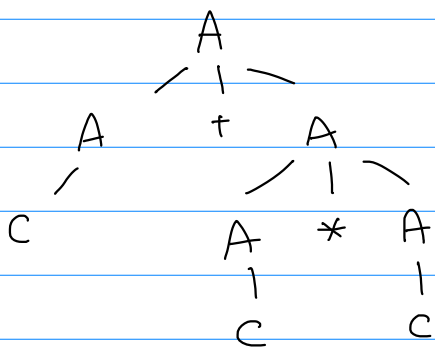
$$A \rightarrow A * A$$

$$A \rightarrow c$$

rightmost derivation

$$A \rightarrow A + A \rightarrow A + A * A$$

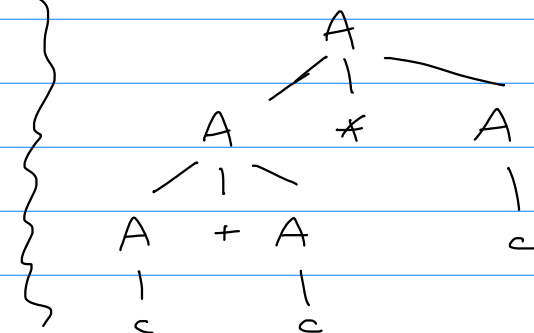
$$\stackrel{*}{\Rightarrow} c + c * c$$



leftmost derivation.

$$A \rightarrow A * A \rightarrow A + A * A$$

$$\stackrel{*}{\Rightarrow} c + c * c$$



2 distinct parse trees \rightarrow AMBIGUOUS Grammar
 Pongling "if"