

value numbering:

Common subexpression, elimination

loop optimization:

B1

B2

B3

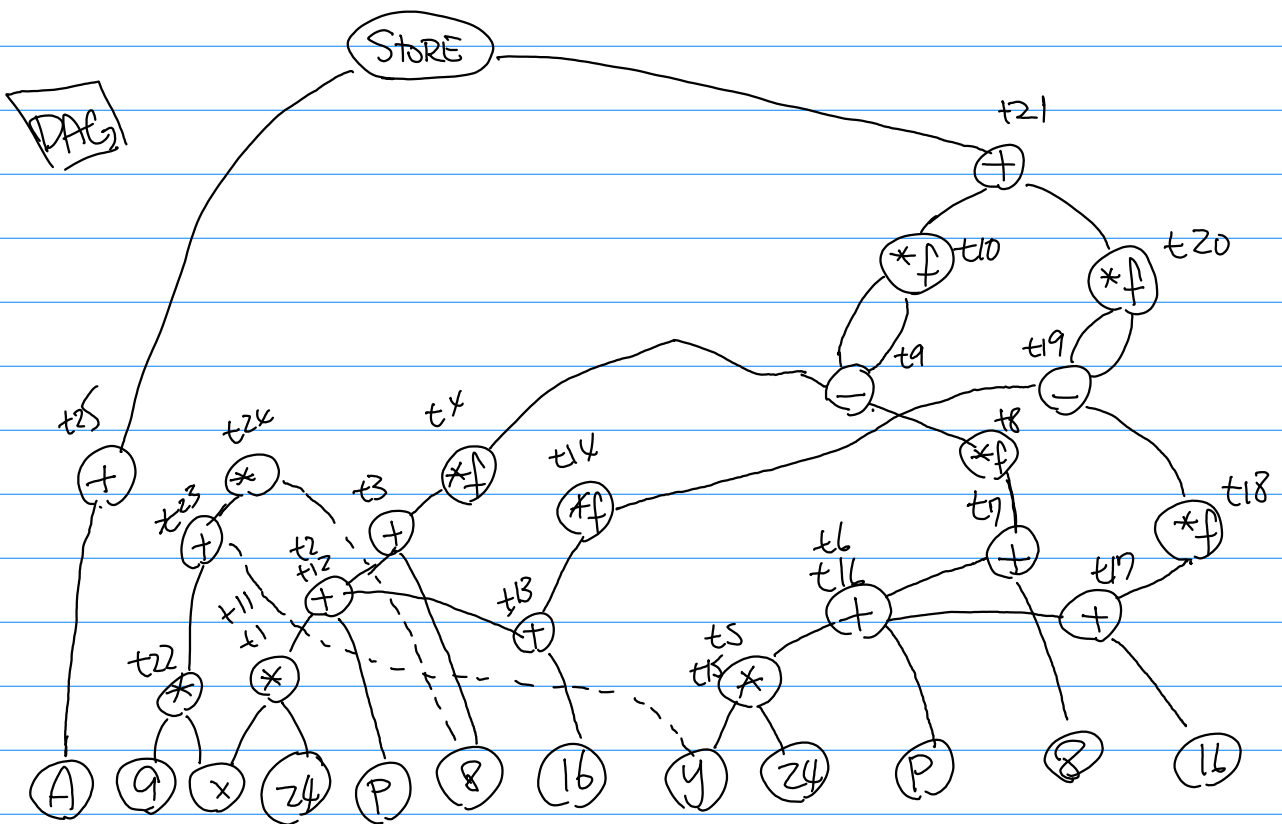
B4

B5

expression DAG for block 3

$x=0$

$y=0$



definitions of all variables

loop invariant → $t1 = x + 24$
 $t2 = t1 * p$
 \vdots

$t3 = t2 + 8$
 $t4 = x + t3$ (f) ← loads and thus not invariant
 $t5 = y * 24$
 ↑
 not invariant, but an index for a loop

$t10 = t9 * t8$
 $t13 = t2 + t6$
 $t14 = *t13$ (f)
 $t17 = t6 + t16$
 $t18 = *t17$ (f)
 \vdots

loop optimizations:

↳ reaching definitions (reachable)

code motion for loop invariants (move loop preheader)

those in the code that can be defined ☺

$[B1, 1, x]$ $[A]$ (defined internally) $[B4, 1, x]$ (local (externally to the y loop) (does not change as y changes))
 $[B2, 1, y]$
 $[B3, 1, t4]$
 $[B3, 2, t2]$

instruction $t53 = opA * opB$
 loop invariant (pointing to the instruction)
 $t4$ is not loop invariant

$y=0$
 ↓
 $t1, t2, t3, t13$: $[B3']$ ← loop preheader
 ↓
 $[B3]$

All outside of loop predecessor of $B3$ now predecessor of $B3'$.

loop induction variables

- have one offsetting assignment in loop.

$$y = y + 1$$

$$z = z + 2 \quad z_0 + 2^* \# \text{ of loop iterations}$$

↓

$$z_0 + 2^* (y - y_0)$$

$$z_0 + 2y - 2y_0$$

$$\underbrace{(z_0 - 2y_0)}_{z'} + 2y$$

$$\begin{cases} y = z_0 + z' \\ z = z_0' + y' \end{cases}$$

$[t5 = t5 + 24]$
Strength reduction
never used

$[t6 = t6 + 24]$ if initialized properly
then $t5$ instruction will be removed as it is not used.

$$[t7 = t7 + 24]$$

$$[t17 = t17 + 24]$$